

# Recitation 2 - P8310 Fall 2017

September 21, 2017

## Problem 1

Let  $A = \{\text{serum cholesterol} = 240 - 289\}$ ,  $B = \{\text{serum cholesterol} \geq 290\}$ ,  $C = \{\text{serum cholesterol} \leq 270\}$ .

- 1) Are the events  $A$  and  $B$  mutually exclusive?
- 2) Are the events  $C$  and  $D$  mutually exclusive?
- 3) Suppose  $P(A) = 0.3$ ,  $P(B) = 0.2$ . What is  $P(\text{serum cholesterol} \geq 250)$ ?
- 4) What does  $A \cup C$  mean?
- 5) What does  $A \cap C$  mean?
- 6) What does the event  $\bar{B}$  mean? What is its probability?

## Problem 2

Two psychological tests aimed at measuring Depression were administered to a sample of individuals. A definitive diagnosis was made using the SCID. The other instrument contained 7 items. The following table provides the distribution of outcomes based on these tests:

Items answered "Yes"	Depressed	Not Depressed
0	0	3
1	1	4
2	5	2
3	7	5
4	11	2
5	20	0
6	30	1
7	34	1

Suppose a cutoff value of  $\geq 5$  on the test is used to identify people with depression.

- 1) What is the sensitivity of the test?
- 2) What is the specificity of the test?

- 3) Suppose we want to develop an ROC curve to reassess the cutoff value for the test. What are the sensitivity and specificity at each of the cutoffs (starting with 1 to 7 items answered "Yes"? Make a table of your results.
- 4) Construct an ROC curve based on the table constructed in question 3).
- 5) Suppose we want both the sensitivity and specificity to be at least 70%. Use the ROC curve to identify the best value(s) to use as the cutoff for identifying people with depression.

### Problem 3

Use the following information to answer the questions below. An experiment is designed to test the potency of a drug on 15 mice. Previous students have shown that a 5 mg dose of the drug is lethal 3% of the time within the first 2 hours; of the animals alive at 2 hours 4% will die within the next two hours.

- 1) What is the probability that at least 3 rats die within the first two hours?
- 2) Suppose 3 rats die within the first two hours, what is the probability that 2 or fewer die in the next two hours?

### Problem 4

Use the following information to answer the questions below. An article was recently published concerning the evidence of a cardiac death attributable to an earthquake in San Francisco on -. In the week before the earthquake there were on average 12.4 cardiac deaths per day in San Francisco. On the day of the earthquake there was 41.

- 1) What is the exact probability of 23 deaths occurring on one day if the cardiac death rate in the previous week continued to hold on the day of the earthquake?
- 2) Is the occurrence of 23 deaths an unusual occurrence?

### Problem 5

Based on an analysis of data collected by the National Center for Health Statistics, it was reported that 19.7 percent of U.S. adults were overweight. If we select a simple random sample of 25 U.S. adults, find the probability that the number of overweight people in the sample will be:

- 1) Exactly 3
- 2) 3 or more
- 3) Fewer than 4
- 4) Between 3 and 7, exclusive
- 5) How many overweight adults would you expect to find in the sample of 25?
- 6) What is the variance of the number of overweight adults in the sample of 25?

## **Problem 6**

Rosner textbook 8<sup>th</sup> edition, 5.21 - 5.24.